You MAY use your calculators.


Let $f$ and $g$ be the functions given by $f(x)=2 x(1-x)$ and $g(x)=3(x-1) \sqrt{x}$ for $0 \leq x \leq 1$. The graphs of $f$ and $g$ are shown in the figure above.
(a) Find the area of the region enclosed by the graphs of $f$ and $g$.
(b) Find the volume of the solid generated when the region enclosed by the graphs of $f$ and $g$ is revolved about the horizontal line $y=2$.
(c) Let $h$ be the function defined by $h(x)=k x(1-x)$ for $0 \leq x \leq 1$. For each $k>0$, the region (not shown) enclosed by the graphs of $h$ and $g$ is the base of a solid with square cross sections perpendicular to the $x$-axis. There is a value of $k$ for which the volume of this solid is equal to 15 . Write, but do not solve, an equation involving an integral expression that could be used to find the value of $k$.

