You MAY NOT use your calculators.

Let $f$ be the function defined by $f(x)=k \sqrt{x}-\ln x$ for $x>0$, where $k$ is a positive constant.
(a) Find $f^{\prime}(x)$ and $f^{\prime \prime}(x)$.
(b) For what value of the constant $k$ does $f$ have a critical point at $x=1$ ? For this value of $k$, determine whether $f$ has a relative minimum, relative maximum, or neither at $x=1$. Justify your answer.
(c) For a certain value of the constant $k$, the graph of $f$ has a point of inflection on the $x$-axis. Find this value of $k$.

